Combining Microarrays and Biological Knowledge for Estimating Gene Networks via Bayesian Networks

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Abstract

We propose a statistical method for estimating a gene network based on Bayesian networks from microarray gene expression data together with biological knowledge including protein-protein interactions, protein-DNA interactions, binding site information, existing literature and so on. Unfortunately, microarray data do not contain enough information for constructing gene networks accurately in many cases. Our method adds biological knowledge to the estimation method of gene networks under a Bayesian statistical framework, and also controls the trade-off between microarray information and biological knowledge automatically. We conduct Monte Carlo simulations to show the effectiveness of the proposed method. We analyze Saccharomyces cerevisiae gene expression data as an application.

1. Introduction

In recent years, a large amount of gene expression data has been collected and estimating a gene network has become one of the central topics in the field of bioinformatics. Several methodologies have been proposed for constructing a gene network based on gene expression data, such as Boolean networks [1, 2, 32, 42], differential equation models [7, 10, 11, 32] and Bayesian networks [13, 14, 17, 18, 20, 22, 23, 37]. Main drawback for the gene network construction from microarray data is that while the gene network contains a large number of genes, the information contained in gene expression data is limited by the number of microarrays, their quality, the experimental design, noise, and measurement errors. Therefore, estimated gene networks contain some incorrect gene regulations, which cannot be evaluated from a biology viewpoint. In particular, the direction of gene regulation is difficult to decide using gene expression data only. Hence, the use of biological knowledge, including protein-protein and protein-DNA interactions [3, 5, 16, 21, 25], sequences of the binding site of the genes controlled by transcription regulators [31, 40, 47], literature and so on, are considered to be a key for microarray data analysis. The use of biological knowledge has previously received considerable attention for extracting more information from microarray data [4, 6, 18, 33, 36, 38, 41].

In this paper, we provide a general framework for combining microarray data and biological knowledge aimed at estimating a gene network by using a Bayesian network model. If the gene regulation mechanisms are completely known, we can model the gene network easily. However, many parts of the true gene network are still unknown and need to be estimated from data. Hence, it is necessary to construct a suitable criterion for evaluating estimated gene



networks in order to obtain an optimal network. While criteria proposed previously for evaluating a Bayesian network model only measure the closeness between a model and microarray data, we derive a criterion for selecting networks based on microarray data and biological knowledge. The proposed criterion is conducted by two components: One shows the fitness of the model to the microarray data and the other reflects biological knowledge, which is modeled under a probabilistic framework. Our proposed method automatically tunes the balance between the biological knowledge and microarray data based on our criterion and estimates a gene network from the combined data. In Section 2.1, we describe our statistical model for constructing gene networks and introduce a criterion for evaluating networks in Section 2.2. A statistical framework for representing biological knowledge is described in Section 2.3. In Section 2.4, we illustrate how to model various types of biological knowledge in practice. Monte Carlo simulations, in Section 3.1, are conducted to show the effectiveness of the proposed method. We apply our method to Saccharomyces cerevisiae gene expression data in Section 3.2.

2. Method for Estimating Gene Networks

2.1. Bayesian network and nonparametric heteroscedastic regression model

Bayesian networks [26] are a type of graphical models for capturing complex relationships among a large amount of random variables by the directed acyclic graph encoding the Markov assumption. In the context of Bayesian networks, a gene corresponds to a random variable shown as a node, while gene regulations are shown by directed edges. Thus gene interactions are modeled by the conditional distribution of each gene. We use Bayesian network and nonparametric heteroscedastic regression models [23] for constructing gene networks from microarray data.

Suppose that we have *n* sets of microarrays $\{x_1, ..., x_n\}$ of *p* genes, where $x_i = (x_{i1}, ..., x_{ip})^T$ is a *p* dimensional gene expression vector obtained by *i*th microarray. Here, x_{ij} is an expression value of *j*th gene, denoted by gene_j, measured by *i*th microarray after required normalizations and transformation [39]. Ordinary, x_{ij} is given by $\log_2(R_{ij}/G_{ij})$, where R_{ij} and G_{ij} are normalized intensities of Cy5 and Cy3 for gene_j measured by *i*th microarray. The interaction between gene_j and its parents is modeled by the nonparametric additive regression model [19] with heterogeneous error variances

$$x_{ij} = m_{j1}(p_{i1}^{(j)}) + \dots + m_{jq_j}(p_{iq_j}^{(j)}) + \varepsilon_{ij},$$

where $p_{ik}^{(j)}$ is the expression value of kth parent of gene_j measured by *i*th microarray and ε_{ij} depends independently

and normally on mean 0 and variance σ_{ij}^2 . Here, $m_{jk}(\cdot)$ is a smooth function constructed by *B*-splines [9, 12, 24] of the form

$$m_{jk}(p_{ik}^{(j)}) = \sum_{m=1}^{M_{jk}} \gamma_{mk}^{(j)} b_{mk}^{(j)}(p_{ik}^{(j)}),$$

where $\{b_{1k}^{(j)}(\cdot), ..., b_{M_{jk},k}^{(j)}(\cdot)\}$ is a prescribed set of *B*-splines and $\gamma_{mk}^{(j)}$ are parameters. Hence, a Bayesian network and nonparametric heteroscedastic regression model can be represented as

$$f(oldsymbol{x}_i;oldsymbol{ heta}_G) = \prod_{j=1}^p f_j(x_{ij}|oldsymbol{p}_{ij};oldsymbol{ heta}_j)$$

for i = 1, ..., n, where θ_G is a parameter vector and $f_j(x_{ij}|p_{ij}; \theta_j)$ is a density of Gaussian distribution with mean $m_{j1}(p_{i1}^{(j)}) + \cdots + m_{jq_i}(p_{iq_j}^{(j)})$ and variance σ_{ij}^2 . If gene_j has no parent genes, we use μ_j and σ_j^2 instead of $m_{j1}(p_{i1}^{(j)}) + \cdots + m_{jq_j}(p_{iq_j}^{(j)})$ and σ_{ij}^2 , respectively. This model has several advantages. Unlike Boolean net-

This model has several advantages. Unlike Boolean networks and discrete Bayesian networks [13, 14, 17, 18, 20, 37], no discretization of gene expression data, which leads to information loss, is required. Second, even nonlinear relationships between genes are automatically extracted based on gene expression data.

2.2. Criterion for evaluating networks

Some gene networks are partially known, but many mechanisms of gene regulations are still unknown. Therefore we need to estimate unknown structures of the gene network from the data. Hence, the construction of a suitable criterion for measuring the closeness between an estimated gene network and the true one is an essential problem for statistical gene network modeling. Following the result of Imoto *et al.* [23], a criterion for evaluating an estimated gene network can be derived from Bayes approach. At first, we briefly introduce the derivation of their criterion. We then explain how extend their criterion for combining microarray data and biological knowledge.

When we construct a gene network G by using a Bayesian network model, the posterior probability of the network is obtained as the product of prior probability of the network $\pi(G)$ and the marginal likelihood divided by the normalizing constant. After dropping the normalizing constant, the posterior probability of the network is proportional to

$$\pi(G) \int \prod_{i=1}^n f(\boldsymbol{x}_i; \boldsymbol{\theta}_G) \pi(\boldsymbol{\theta}_G | \boldsymbol{\lambda}) d\boldsymbol{\theta}_G,$$



where $\pi(\theta_G|\boldsymbol{\lambda})$ is a prior distribution on the parameter vector θ_G with hyperparameter vector $\boldsymbol{\lambda}$ satisfying $\log \pi(\theta_G|\boldsymbol{\lambda}) = O(n)$. The essential problem for constructing a criterion based on the posterior probability of the network is how to compute the marginal likelihood given by a high dimensional integral. Imoto *et al.* [23] used the Laplace approximation for integrals [8, 30, 45] and derived a criterion, named BNRC_{hetero} (<u>Bayesian network and Nonparametric heteroscedastic Regression Criterion</u>), of the form

$$BNRC_{hetero}(G) = -2\log \pi(G) + \log \left| \frac{n}{2\pi} J_{\lambda}(\hat{\boldsymbol{\theta}}_{G}) \right| - 2n l_{\lambda}(\hat{\boldsymbol{\theta}}_{G} | \boldsymbol{X}),$$

where

$$l_{\lambda}(\boldsymbol{\theta}_{G}|\boldsymbol{X}) = \frac{1}{n} \sum_{i=1}^{n} \log f(\boldsymbol{x}_{i};\boldsymbol{\theta}_{G}) + \frac{1}{n} \log \pi(\boldsymbol{\theta}_{G}|\boldsymbol{\lambda}),$$
$$J_{\lambda}(\boldsymbol{\theta}_{G}) = -\frac{\partial^{2} \{l_{\lambda}(\boldsymbol{\theta}_{G}|\boldsymbol{X})\}}{\partial \boldsymbol{\theta}_{G} \partial \boldsymbol{\theta}_{G}^{T}}$$

and $\hat{\boldsymbol{\theta}}_{G}$ is the mode of $l_{\lambda}(\boldsymbol{\theta}_{G}|\boldsymbol{X})$.

Suppose that the prior distribution $\pi(\theta_G|\boldsymbol{\lambda})$ is factorized as

$$\pi(\boldsymbol{\theta}_{G}|\boldsymbol{\lambda}) = \prod_{j,k} \pi_{jk}(\boldsymbol{\gamma}_{jk}|\boldsymbol{\lambda}_{jk}),$$

where $\gamma_{jk} = (\gamma_{1k}^{(j)}, ..., \gamma_{M_{jk},k}^{(j)})^T$ is a parameter vector and λ_{jk} is a hyperparameter. We use a singular M_{jk} variate normal distribution as the prior distribution on γ_{jk} ,

$$\pi_{jk}(\boldsymbol{\gamma}_{jk}|\lambda_{jk}) = \left(\frac{2\pi}{n\lambda_{jk}}\right)^{-(M_{jk}-2)/2} |K_{jk}|_{+}^{1/2} \times \exp\left(-\frac{n\lambda_{jk}}{2}\boldsymbol{\gamma}_{jk}^{T}K_{jk}\boldsymbol{\gamma}_{jk}\right),$$

where K_{jk} is an $M_{jk} \times M_{jk}$ symmetric positive semidefinite matrix satisfying $\gamma_{jk}^T K_{jk} \gamma_{jk} = \sum_{\alpha=3}^{M_{jk}} (\gamma_{\alpha k}^{(j)} - 2\gamma_{\alpha-1,k}^{(j)} + \gamma_{\alpha-2,k}^{(j)})^2$. Then we have the decomposition $\text{BNRC}_{hetero} = -2 \log \pi(G) + \sum_{j=1}^{p} \text{BNRC}_{hetero}^{(j)}$. Here $\text{BNRC}_{hetero}^{(j)}$ is a score for gene_j and given by

BNRC^(j)_{hetero} =
$$-(\sum_{k=1}^{q_j} M_{jk} + 1) \log(\frac{2\pi}{n})$$

 $-\sum_{i=1}^{n} \log w_{ij} + n \log(2\pi\hat{\sigma}_j^2) + n$
 $+\sum_{k=1}^{q_j} \{\log |\Lambda_{jk}| - M_{jk} \log(n\hat{\sigma}_j^2)\}$



Figure 1. A gene network and its energy. The index sets L_3 , L_4 and L_5 are illustrated and L_1 and L_2 are defined by empty sets. The local energies are $E_3 = U_{13}$, $E_4 = U_{24}$ and $E_5 = U_{35} + U_{45}$. The total energy of this network is $E = E_3 + E_4 + E_5 = U_{13} + U_{24} + U_{35} + U_{45}$.

$$-\log(2\hat{\sigma}_{j}^{2}) - \log|K_{jk}|_{+}$$

$$+ \sum_{k=1}^{q_{j}} \{(M_{jk} - 2) \log\left(\frac{2\pi\hat{\sigma}_{j}^{2}}{n\beta_{jk}}\right)$$

$$+ \frac{n\beta_{jk}}{\hat{\sigma}_{j}^{2}}\hat{\gamma}_{jk}^{T}K_{jk}\hat{\gamma}_{jk}\}$$

where w_{ij} , i = 1, ..., n are weights of the heterogeneous error variance $\sigma_{ij}^2 = w_{ij}^{-1}\sigma_j^2$ and $\Lambda_j = B_{jk}^T W_j B_{jk}$ $+n\beta_{jk}K_{jk}$ with $B_{jk} = (\mathbf{b}_{jk}(p_{1k}^{(j)}), ..., \mathbf{b}_{jk}(p_{nk}^{(j)}))^T$, $\mathbf{b}_{jk}(p_{ik}^{(j)}) = (b_{1k}^{(j)}(p_{ik}^{(j)}), ..., b_{M_{jk},k}^{(j)}(p_{ik}^{(j)}))^T$, $W_j =$ diag $(w_{1j}, ..., w_{nj})$ and $\beta_{jk} = \sigma_j^2 \lambda_{jk}$. The details of the parameter estimation are described in Imoto *et al.* [23].

2.3. Adding biological knowledge

The criterion BNRC_{hetero}(G), introduced in the previous section, contains two quantities: the prior probability $\pi(G)$ of the network, and the marginal likelihood of the data. The marginal likelihood shows the fitness of the model to the microarray data. The biological knowledge can then be added into the prior probability of the network $\pi(G)$.

Let U_{ij} be the interaction energy of the edge from gene_i to gene_j and let U_{ij} be categorized into I values, H_1, \ldots, H_I , based on biological knowledge. For example, if we know *a priori* gene_i regulates gene_j, we set $U_{ij} = H_1$. However, if we do not know whether gene_k regulates gene_l or not, we set $U_{kl} = H_2$. Note that $0 < H_1 < H_2$. The



total energy of the network G can then be defined as

$$E(G) = \sum_{\{i,j\}\in G} U_{ij},$$

where the sum is taken over the existing edges in the network G. Under the Bayesian network framework, the total energy can be decomposed into the sum of the local energies

$$E(G) = \sum_{j=1}^{p} \sum_{i \in L_j} U_{ij} = \sum_{j=1}^{p} E_j, \qquad (1)$$

where L_j is an index set of parents of gene_j and $E_j = \sum_{i \in L_j} U_{ij}$ is a local energy defined by gene_j and its parents. Figure 1 shows an example of a gene network and its energy.

The probability of a network G, $\pi(G)$, is naturally modeled by the Gibbs distribution [15]

$$\pi(G) = Z^{-1} \exp\{-\zeta E(G)\},$$
(2)

where ζ (> 0) is a hyperparameter and Z is a normalizing constant called the partition function

$$Z = \sum_{G \in \mathcal{G}} \exp\{-\zeta E(G)\}.$$

Here \mathcal{G} is the set of possible networks. By replacing $\zeta H_1, \ldots, \zeta H_I$ with ζ_1, \ldots, ζ_I , respectively, the normalizing constant Z is a function of ζ_1, \ldots, ζ_I . We call ζ_j an inverse normalized temperature. By substituting (1) into (2), we have

$$\pi(G) = Z^{-1} \prod_{j=1}^{p} \exp\{-\zeta E_{j}\} = Z^{-1} \prod_{j=1}^{p} \prod_{i \in L_{j}} \exp(-\zeta_{\alpha(i,j)}),$$

with $\alpha(i, j) = k$ for $U_{ij} = H_k$. Hence, by adding biological knowledge into the prior probability of the network, BNRC_{hetero} can be rewritten as

$$BNRC_{hetero}(G, \zeta_1, ..., \zeta_I) = 2 \log Z + \sum_{j=1}^{p} \{2 \sum_{i \in L_j} \zeta_{\alpha(i,j)} + BNRC_{hetero}^{(j)} \}.$$
(3)

We can choose an optimal network under the given $\zeta_1, ..., \zeta_I$. Also the optimal values of $\zeta_1, ..., \zeta_I$ are obtained as the minimizer of (3). Therefore, we can represent an algorithm for estimating a gene network from microarray data and biological knowledge as follows:

Step1: Set the values $\zeta_1, ..., \zeta_I$.

Step2: Estimate a gene network by minimizing BNRC_{h etero}(G) under the given $\zeta_1, ..., \zeta_I$.

Step3: Repeat Step1 and Step2 against the candidate values of $\zeta_1, ..., \zeta_I$.

Step4: An optimal gene network is obtained from the candidate networks obtained in Step3.

In Step2, we use the greedy hill-climbing algorithm for learning networks. The details are shown in Imoto *et al.* [23]. Note that the proposed prior probability of the network can be used for other types of Bayesian network models, such as discrete Bayesian networks and dynamic Bayesian networks [29, 34, 36, 43].

The computation of partition function, Z, is intractable even for moderately sized gene networks. To avoid this problem, we compute upper and lower bounds of the partial function and use them for choosing the optimal values of ζ_1, \ldots, ζ_I . An upper bound is obtained by directed graphs, which are allowed to contain cyclic graphs. Thus the true value of the partition function is not greater than the upper bound. A lower bound is computed by multi-level directed graphs with following assumptions: (A1) There is one top gene and (A2) Genes at the same level have a common parent gene that is located on one upper level of them. We also consider joined graphs of some multi-level directed graphs satisfying (A1) and (A2). Since the number of possible graphs is much larger than those included in the computation, the true value of the partition function should be greater than the lower bound. Since the optimization of the network structure for fixed ζ_1, \ldots, ζ_I does not depend on the value of the partition function, our method works well in practice. Of course, when the number of genes is small, we can perform an exhaustive search and compute the partition function completely. However, we think that the development of an effective algorithm to enumerate all possible networks or approximate the partition function is an important problem.

2.4. Prior design for various biological knowledge

In this subsection, we show some examples of biological knowledge and how to include them into the prior probability in practice. We consider using two values ζ_1 and ζ_2 satisfying $0 < \zeta_1 < \zeta_2$ for representing biological knowledge. Basically, we allocate ζ_1 to a known relationship and ζ_2 otherwise. The prior information can be summarized as a $p \times p$ matrix U whose (i, j) element, u_{ij} , corresponds to ζ_1 or ζ_2 .

Protein-protein interactions

The number of known protein-protein interactions is rapidly increasing and kept in some public databases such





Figure 2. Artificial gene network and functional structures between nodes.

as GRID [16] and BIND [3, 5]. Protein-protein interactions show at least two proteins form a complex. Therefore, representing protein-protein interactions by a directed graph is not suitable. However, they can be included in our method. If we know gene_i and gene_j create a protein-protein interaction, we set $u_{ij} = u_{ji} = \zeta_1$. In such a case, we will decide whether we make a virtual node corresponding to a protein complex theoretically [35].

Protein-DNA interactions

Protein-DNA interactions show gene regulations by transcription factors and can be modeled more easily than protein-protein interactions. When gene_i is a transcription regulator and controls gene_j, we set $u_{ij} = \zeta_1$ and $u_{ji} = \zeta_2$.

Sequences

Genes that are controlled by a transcription regulator might have a consensus motif in their promoter DNA sequences. If gene_{j1},...,gene_{jn} have a consensus motif and are controlled by gene_i, we set $u_{ij_1} = \cdots = u_{ij_n} = \zeta_1$ and $u_{j_1i} = \cdots = u_{j_ni} = \zeta_2$. Previously, consensus motifs were often used for the evaluation of estimated gene networks from a biological viewpoint. This information, however, can be introduced directly into our method. One straightforward way is the use of known regulatory motifs kept in public databases such as SCPD [40] and YTF [47]. As for an advanced method, Tamada *et al.* [44] proposed a method for simultaneously estimating a gene network and detecting regulatory motifs based on our method, and succeeded in estimating an accurate gene network and detecting a true regulatory motif.

Gene networks and pathways

The information of gene networks can be introduced

directly into our method by transforming the prescribed network structures into the matrix U. We can then estimate a gene network based on U and microarray data. Our method also can use gene networks estimated by other techniques such as boolean networks, differential equation models, and so on. Also, some databases, such as KEGG [28], contain several known gene networks and pathways. This information can be used similarly.

Literature

Some research has been performed to extract information from a huge amount of literature [27]. Literature contain various kinds of information including biological knowledge described above. So we can model literature information in the same way.

3. Computational Experiments

3.1. Monte Carlo simulations

Before analyzing real gene expression data, we perform Monte Carlo simulations to examine the properties of the proposed method. We assume an artificial network with 20 nodes shown in Figure 2 (a). The functional relationships between nodes are listed in Figure 2 (b). A network will be rebuilt from simulated data consisting of 50 or 100 observations, which corresponds to 50 or 100 microarrays. As for the biological knowledge, we tried the following situations: (**Case 1**) we know some gene regulations (100%, 75%, 50% or 25% out of 19 edges shown in Figure 2 (a)) and (**Case 2**) we know some gene regulations, but some (1, 2, or 3) incorrect edges are kept in the database. The candidate values of ζ_1 and ζ_2 are {0.5, 1.0} and { ζ_1 , 2.5, 5.0, 7.5, 10.0}, respectively.





Figure 3. The behavior of BNRC_{hetero} when ζ_1 = 0.5. We can find out the optimal inverse normalized temperature ζ_2 is 5.0.

Figure 4 shows two estimated networks: One is estimated by 100 observations (microarrays) alone. We use $\zeta_1 = \zeta_2 = 0.5$, i.e. we did not use any knowledge (we denote this network by N_0 for convenience). The other is estimated by 100 observations and prior information of 75% gene regulations, i.e. we know 14 correct relations out of the all 19 correct edges (we denote this network by N_1). Edges appearing in both networks are colored green, while edges appearing in N_0 or N_1 only are colored blue and red, respectively. By adding prior knowledge, it is clear that we succeeded in reducing the number of false positives. We also find additional four correct relationships. Figure 3 shows the behavior of BNRC_{hetero} when $\zeta_1 = 0.5$. We find that the optimal value of ζ_2 is 5.0. From the Monte Carlo simulations, we observed that ζ_2 can be selected by using middle values (depicted by a blue line) of upper and lower bounds or upper bounds in practice. For the selection of ζ_1 , we use the middle value of the upper and lower bounds of the score of our criterion.

The results of the Monte Carlo simulations are summarized as follows:

In (**Case 1**), we obtained networks more accurately as long as we add correct knowledge. We observed that the number of false positives decreased drastically. We presume the reason is the nature of directed acyclic graphs. Since a Bayesian network model is a directed acyclic graph, one incorrect estimate may affect the relations in its neighborhood. However, by adding some correct knowledge, we



Figure 4. An example of resulting networks based on 100 samples. We used $\zeta_1 = 0.5$ and $\zeta_2 = 5.0$ that are selected by our criterion (see Figure 3).

can restrict the search space of the Bayesian network model learning effectively.

In (Case 2), the results depend on the type of incorrect knowledge.

(i) If we use misdirected relations, e.g. $gene_8 \rightarrow gene_3$, as prior knowledge, serious problems occur. Since microarray data to some degree support the misdirected relations, they tend to receive a better criterion score.

(ii) If we add indirect relations such as gene₁ \rightarrow gene₈, we observed that our method controlled the balance between this prior information and microarray data and could decide whether the prior relation is true.

(iii) If irrelevant relations such as gene₂₀ \rightarrow gene₅ are added as prior information, we observed that our method could reject these prior information, because, the microarray data do not support these relations.

3.2. Example using experimental data

In this subsection, we demonstrate our method by analyzing *Saccharomyces cerevisiae* gene expression data obtained by disrupting 100 genes, which are almost all transcription factors. We focus on five genes, *MCM1*, *SWI5*, *ACE2*, *SNF2* and *STE12* (see Table 1) and extract genes that are regulated by these 5 genes from the Yeast Proteome Database [46]. Thus, we construct a prior network shown in Figure 5, based on the database information. We include the prior network in our Bayesian network estimation method.



<i>MCM1</i> : transcription factor of the MADS box family
MET14, CDC6, MET2, CDC5, MET6, SIC1, STE6, CLN2, PCL2, STE2, ACE2, MET16,
MET3, MET4, CAR1, SWI5, PCL9, CLB1, MET17, EGT2, ARG5,6, PMA1, RME1, CLB2
SWI5 : transcription factor
CDC6, SIC1, CLN2, PCL2, PCL9, EGT2, RME1, CTS1, HO
ACE2: metallothionein expression activator
CLN2, EGT2, HO, CTS1, RME1
SNF2: component of SWI/SNF global transcription activator complex
CTS1, HO
STE12: transcriptional activator
STE6, FAR1, KAR3, SST2, FUS1, STE2, BAR1, AGA1, AFR1, CIK1

Table 1. Five transcription factors and their regulating genes.



Figure 5. Prior knowledge network. The genes that are in each shadowed circle are regulated by the parent genes.

That is, the purpose of this analysis is to estimate the gene network containing above 36 genes from microarray data together with the prior network. Figure 6 shows the estimated gene network using microarray data only. There are many non-prior edges and many of them are probably false positives. In addition, we find three misdirected relations: "SWI5 \rightarrow MCM1", "HO \rightarrow ACE2" and "STE6 \rightarrow STE12". By adding the prior network, we obtain the gene network shown in Figure 8. As for the inverse normalized temperatures ζ_1 and ζ_2 , we set $\zeta_1 = 0.5$ and choose the optimal value of ζ_2 . We also estimated a gene network based on $\zeta_1 = 1$ and found the results described below to be essentially unchanged.

Figure 7 shows the behavior of BNRC_{hetero} with respect to ζ_2 . We find that the optimal value of ζ_2 is 2.5. Fig-



Figure 6. Resulting network based on microarray only.

ure 8 shows the resulting network based on microarray data and the biological knowledge represented by the prior network in Figure 5. We show the edges that correspond to the prior knowledge in black. The edges between genes that are regulated by the same transcription factor in the prior network are shown in blue. The red edges do not correspond to the prior knowledge. In particular, we find that the relationships around *MCM1* improve drastically. The network based on microarray only (Figure 6) indicates that only <u>SIC1</u> and <u>ACE2</u> are regulated by *MCM1*. Note that the underlined genes correspond to the prior network information. After adding the prior knowledge and optimizing the inverse normalized temperatures, we find that 10 genes out of 24 genes that are listed as co-regulated genes of *MCM1* in Table 1 are extracted. Also, the relationships around *STE12*







Figure 7. Optimization of ζ_2 . We can find out that the optimal value of ζ_2 is 2.5.

Figure 8. Resulting network based on microarray data and biological knowledge. The inverse normalized temperatures are selected by our criterion (ζ_1 =0.5, ζ_2 =2.5).

become clearer. Before adding prior knowledge, the estimated network in Figure 6 suggests <u>FUS1</u>, <u>AFR1</u>, <u>KAR3</u>, <u>BAR1</u>, MET4, MET16 and MCM1 are regulated by STE12, while STE12 is controlled by HO, STE6 and MET3. On the other hand, the network in Figure 8 shows that STE12 regulates <u>FUS1</u>, <u>AFR1</u>, <u>KAR3</u>, <u>CIK1</u>, <u>STE2</u>, <u>STE6</u>, HO and MCM1. Note that the three misdirected relations described above are corrected in Figure 8. The difference between the inverse normalized temperatures $\zeta_1 = 0.5$ and $\zeta_2 = 2.5$ is small, because the score of the criterion is added as $2\zeta_1$ or $2\zeta_2$, when we add an edge that is listed or not listed in the prior network, respectively. Therefore, microarray data contain this information and we succeeded in extracting this information with the slight help of the prior network.

We optimized the inverse normalized temperature ζ_2 based on the proposed criterion. From the network based on the optimal inverse normalized temperatures, we can find the gap between microarray data and biological knowledge. By comparing Figure 6 with Figure 8, we find that the microarray data reflect the relationship between seven genes (*CLN2*, *RME1*, *CDC6*, *EGT2*, *PCL2*, *PCL9* and *SIC1*) and two transcription factors (*MCM1* and *SWI5*). On the other hand, we find that there are somewhat large differences between microarray data and the prior network for the relationship between *MCM1* and the thirteen genes that are in the biggest circle.

4. Discussion

In this paper we proposed a general framework for combining microarray data and biological knowledge aimed at estimating a gene network. An advantage of our method is the balance between microarray information and biological knowledge is optimized by the proposed criterion. By adding biological knowledge into our Bayesian network estimation method, we succeeded in extracting more information from microarray data and estimating the gene network more accurately. We believe that the combination of microarray data and biological knowledge gives a new perspective for understanding the systems of living creatures.

We consider the following problems as our future works: (1) In the real application, we demonstrated how to use the gene network that is obtained biologically as a prior knowledge. There are various types of biological knowledge we listed in Section 2.4. It is a very important problem how to use such knowledge together with microarray data in practice. (2) From biological knowledge, we deterministically decided the category to which edges belong, e.g. $u_{11} = \zeta_1$, $u_{12} = \zeta_2$, and so on. However, biological knowledge contains some errors. In fact, u_{ij} can be viewed as a random variable, and a statistical model can be constructed for u_{ij} . In that sense, our method can be extended as a Bayesian network estimation method with a self-repairing database mechanism. We would like to investigate these problems in a future paper.



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